

### Formulas for mathematics:

Line through point  $(s, t)$  with slope  $a$ :  $y - t = a(x - s)$

Line through points  $(s_1, t_1)$  and  $(s_2, t_2)$ :  $y - t_1 = \frac{t_2 - t_1}{s_2 - s_1}(x - s_1)$

$$f(x) = ax^2 + bx + c = 0 \quad \text{for} \quad x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Inverses:

$$\begin{aligned} f(x) &= x^a & f^{-1}(y) &= y^{1/a} & (a \neq 0; x, y > 0) \\ f(x) &= a^x & f^{-1}(y) &= {}^a\log y & (a > 0) \end{aligned}$$

Important derivatives

$$\begin{aligned} f(x) &= x^a & f'(x) &= ax^{a-1} & (a \neq 0) \\ f(x) &= a^x & f'(x) &= a^x \ln a & (a > 0) \\ f(x) &= {}^a\log x & f'(x) &= \frac{1}{x \ln a} & (a > 0) \end{aligned}$$

Rules for derivatives

Let  $f'(x)$  and  $g'(x)$  exist, then

| Operation   | Function            | Derivative                             |
|-------------|---------------------|----------------------------------------|
| Sum         | $f(x) \pm g(x)$     | $f'(x) \pm g'(x)$                      |
| Product     | $f(x) \cdot g(x)$   | $f'(x) \cdot g(x) + f(x) \cdot g'(x)$  |
| Quotient    | $\frac{f(x)}{g(x)}$ | $\frac{g(x)f'(x) - f(x)g'(x)}{g^2(x)}$ |
| Composition | $f(g(x))$           | $f'(g(x))g'(x)$                        |

Relative rate of increase:  $\frac{f'(x)}{f(x)}$

Elasticity:  $EL_x f(x) = \frac{x}{f(x)} f'(x)$

Let  $f(x, y)$  have a stationary point  $(x_0, y_0)$

$$\begin{aligned} \text{Minimum} & \quad f_{xx}(x_0, y_0) > 0 \quad f_{yy}(x_0, y_0) > 0 \quad f_{xx}f_{yy} - (f_{xy})^2 > 0 \\ \text{Maximum} & \quad f_{xx}(x_0, y_0) < 0 \quad f_{yy}(x_0, y_0) < 0 \quad f_{xx}f_{yy} - (f_{xy})^2 > 0 \\ \text{Saddle - point} & \quad f_{xx}f_{yy} - (f_{xy})^2 < 0 \end{aligned}$$